

Electric Currents, Resistivity, Ohm's Law

An applied potential difference (voltage) in a conductor creates an electric field.

When current flows in conductor, electrons flow but the ions are "frozen" and don't move

Electrons feel electric field then electrons try to make E-field zero but don't succeed bc of potential diff applied across conductor

Ohm's Law Example:

Consider conductor, say copper (Cu), at room temp (300K), the free electrons in Cu move at 10^6 m/sec. The time between collisions is about $\tau = 3 \times 10^{-19}$ sec.

The number of free electrons per cubic meter is $n = 10^{29} / \text{m}^3$

If we apply a potential difference across conductor then electrons experience force:

$$F = qE$$

and they accelerate as

$$a = \frac{F}{m_e}$$

and they pick up speed on collisions called drift velocity

$$v_d = a\tau$$

So we can solve for drift velocity

$$v_d = \frac{qE}{m_e} \tau$$

Now consider 10m copper wire and we apply potential difference of 10V. The drift velocity of free electrons is.

We know $E = \frac{\Delta V}{d} = \frac{10V}{m} = 1 \frac{V}{m}$

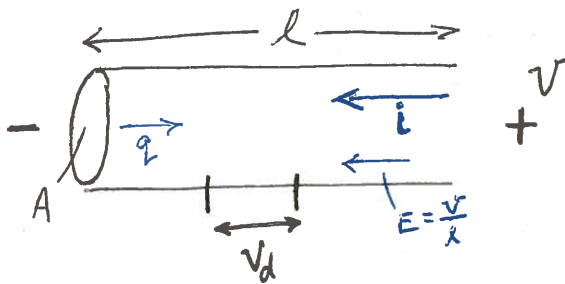
then $v_d = \frac{1.6 \times 10^{-19} C \times 1 \frac{V}{m} \times 3 \times 10^{-14} s}{10^{-30} kg}$

$$\approx 5 \times 10^{-3} m/s$$

$$= \frac{1}{2} \text{ centi-meter/sec}$$

The free electrons move at a million m/s but due to electric field the electrons only travel at .5 cm/s along the wire. Takes 30 min to travel 10m!

Ohm's Law (for conductors)



We want to measure the # electrons through cross-section per second:

$$I = \underbrace{v_d A}_{\text{volume}} \cdot \underbrace{n}_{\text{\# electrons per m}^3} \cdot \underbrace{q}_{\text{charge}}$$

$$I = \frac{q^2 n \tau}{m_e} A E$$

$\frac{q^2 n \tau}{m_e}$

 Conductivity
 (property of conductor)
 $[\sigma]$

If we continue to simplify our expression for current we see

$$I = \sigma A \frac{V}{l}$$

And we can solve for the potential difference

$$V = \underbrace{\frac{l}{\sigma A}}_{\substack{\text{Resistivity} \\ [R]}} I$$

$$R = \frac{l}{\sigma A} = \frac{\rho l}{A}$$

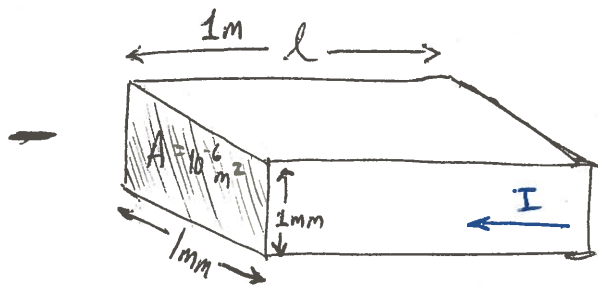
$$[R] = [\Omega]$$

And we get Ohm's Law: $V = IR$

Resistance ($R = \frac{\rho l}{A}$) is directly proportional to length and inversely proportional to area!

As temp increases, so does resistance!

Conductors vs Insulators



$+ V = 1\text{V}$ Apply potential difference across chunk of material. A current flows.

1. Say good conductor... $\sigma \approx 10^8 \rightarrow \rho = 10^{-8}$

$$R = \frac{l}{\sigma A} = \frac{1\text{m}}{10^8 \cdot 10^{-6}} = \underline{10^{-2} \Omega}$$

$$I = \frac{V}{R} = \underline{100\text{A}}$$

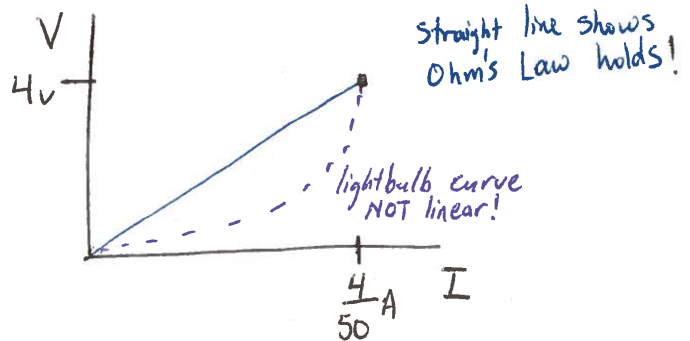
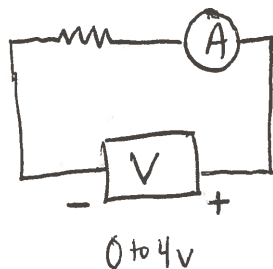
2. Say good insulator $\sigma \approx 10^{-12}$ to 10^{-16}

$$R = \frac{l}{\sigma A} = \frac{1\text{m}}{10^{-14} \cdot 10^{-6}} = \underline{10^{20} \Omega}$$

$$I = \frac{V}{R} = \underline{10^{-20}\text{A}}$$

Huge difference between conductor and insulator!

DEMO:



If we swap resistor w/ lightbulb where $R_{\text{cold}} = 7\Omega$, $R_{\text{hot}} = 50\Omega$ the resistance is not linear! It is a function of temperature.

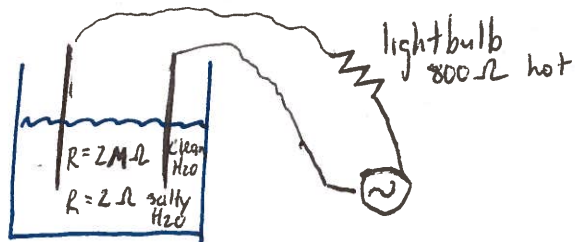
Conductivity increases w/ # of charge carriers (electrons)

DEMO Increase ions by heat

Charge electroscope. Electrons cannot go out into air, they stay. When we heat the surrounding air (w/ candle) we ionize the air and the electrons/ions allow charge to dissipate

Demo Increase ions by salt

Conductivity of water is low $\approx 2 \times 10^5 \Omega m$ but the conductivity of salt water is high!



- Cannot see light when water is clean, resistance is too high!
- but can see light when salt introduced bc resistance is low!